

Journal of Molecular Catalysis A: Chemical 192 (2003) 203-216



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# Modeling MoS<sub>2</sub> catalytic surface with simple clusters

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Received 11 March 2002; accepted 9 July 2002

### Abstract

Theoretical calculations using a modified version of CNDO/UHF method to correct binding energies were carried out on a series of linear  $Mo_x S_y$  (x = 3; y = 6, 8, 10, 12, 14 and x = 5; y = 12, 14) and non-linear (x = 3, y = 6, 8, and x = 5, y = 6, 8, 10, 12, 14, 16, 18, 20) clusters. Results show the formation of  $S_2^-$  species on the surface and the existence of a Mo–Mo interaction. The HOMO orbitals are localized on mono-coordinate S atoms which shows that these atoms have electron-donating properties while the LUMO orbital is delocalized over all coordinatively unsaturated Mo atoms which presents electron-acceptor properties. It is shown that the non-linear clusters are better models for representation of  $MoS_2$  catalysts, because they of their stability respect to the linear clusters.

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Keywords: Parametric method; HDS; MoS2; CNDO-UHF; Vacancies; Cluster

# 1. Introduction

It is well-known that the hydrodesulfurization (HDS) of hydrocarbons is an important catalytic process in the purification of petroleum products due to the high organosulfur compounds content in the heavy oil [1–8]. Different hydrogenation reactions occurs during the HDS processes such as

 $RSH + H_2 \rightarrow RH + H_2S \tag{1}$ 

$$RSR + 2H_2 \rightarrow 2RH + H_2S \tag{2}$$

$$RSSR + 3H_2 \rightarrow 2RH + 2H_2S \tag{3}$$

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Usually, industrial catalysts employed in hydrodesulfurization reactions are composed by molybdenum or tungsten sulfides supported on alumina and promoted with Ni or Co. These catalysts are complex because their highly anisotropic layered structure. Commonly, they are seen as slabs with a MoS<sub>2</sub>-like structure and few layers. It is now agreed that the active sites are located at the edges of the lamellar structure, and the properties of the unsupported catalysts are roughly similar to those of supported systems. Thus, the problem of interaction between the active phase and the support can be avoided using an unsupported solids model [5,9]. Besides the hydrodesulfurization, the MoS<sub>2</sub> and its derivatives are also used in other catalytic reactions, such as isomerization [10], hydrogenation [11], methanation [12], Fischer–Tropsch [13], alcohol synthesis [14], hydrodenitrogenation (HDN) [15], coal liquefaction [16],

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in lubricant uses [17] and in nanotube technology [18]. Furthermore, this material is noteworthy due to its optical, magnetic, superconductive and electrical properties, etc. [19–21]. However, the chemical properties of Mo–S bonds in the microscopic structure are not well-known. Nevertheless, it is known what these properties depend on crystal plane, metal oxidation state, and surroundings [22–35]. All of these factors have strong influence on active sites that are associated with the anionic vacancies of the MoS<sub>2</sub> catalyst. These vacancies are formed on the MoS<sub>2</sub> catalyst during the pretreatment with H<sub>2</sub> or H<sub>2</sub>/H<sub>2</sub>S [36–38].

Quantum chemistry methods based on the neglect differential overlap (NDO) philosophy have been applied to catalytic reactions on transition metals [39–41]. However, these methods depends essentially on how well simulated the parametric functionals are. These parametric functionals are used to evaluate the components of the total energy expression [42-46]and the improvement of these methods is a difficult task because, the parametric functionals must obey the correct asymptotic behavior and the energy components must follow the basic theorems of quantum chemistry [46]. In addition, parameterization for transition metal systems is a very complicated process [43,47], because it has to deal with open shell systems in which several electronic states lay very close in energy. Nevertheless, it is possible to obtain reliable results without a deep parameterization using convenient theoretical tools. For example, a very reasonable evaluation of the interaction energies between atoms in a molecular system can be obtained by the calculation of parameterized diatomic binding energies [48].

In this work, we model the  $MoS_2$  catalytic surface using  $Mo_xS_y$  discrete structures. The quantum chemistry behavior of the Mo–S bond in relation with its position into the molecular structure, the Mo oxidation state, the effect of S neighboring atoms, HOMO, and LUMO are analyzed.

#### 2. Computational and theoretical details

A parametric method based on CNDO-UHF [49] was employed in this work. This includes several modifications [50,51] such as the calculation of diatomic binding energies and Mülliken population with orthogonal molecular orbitals, using the symmetric

transformation of the orbitals. The standard atomic set of parameters employed herein is well described in a previous work [52].

It is well-known that CNDO overestimates binding energies [53,54]. Therefore, in order to amend the calculation of the total energy ( $E_T$ ) and diatomic binding energies (DBE), a new parameterization per each bond was done. This new parameterization let to calculate reasonable total binding energies (TBE) based on a partition scheme of the TBE [52].

The  $E_{\rm T}$  can be calculated in terms of parameterized DBEs (PDBEs) [55] as follows:

$$E_{\rm T} = \sum_{\rm A} \varepsilon_{\rm A}^0 + \sum_{\rm A>B} \rm PDBE(A-B)$$
(4)

$$PDBE(A-B) = \alpha_{AB}DBE(A-B)$$
(5)

and

$$\Gamma BE = E_{\rm T} - \sum_{\rm A} \varepsilon_{\rm A}^0 \tag{6}$$

where  $\varepsilon_A^0$  corresponds to the energy of the free atom A. The parameters  $\alpha_{AB}$  were obtained from the ratio between the accurate value (experimental or theoretical) of the bond dissociation energy (BDE) and the calculated DBE of the correspondent bond of the diatomic or polyatomic molecule, i.e.  $\alpha_{AB}$  = BDE(A-B)/DBE(A-B). The values of the calculated parameters  $\alpha_{AB}$  used herein are:  $\alpha_{Mo-Mo} = 0.77$ ,  $\alpha_{S-S} = 0.77$ , and  $\alpha_{Mo-S} = 0.52$ . The  $\alpha_{AB}$  values were obtained using BDE data taken from theoretical and experimental data [56-58]. As expected, this approach only gives semi-quantitative results, for example, the PDBE(C-H) for CH<sub>4</sub> and CH<sub>3</sub> molecules are 99.6 and 114.3 kcal/mol, respectively compared with the experimental values of 101.6 and 112.3 kcal/mol [59].

#### 3. Surface model

It is well-known that the  $MoS_2$  crystallite size depends on the preparation method. Normally, the crystallites size in ultra disperse particles is between 10 and 50 Å, for example, in those catalysts prepared by anchoring Mo complexes [3,60–62]. In catalysts prepared by impregnation, the particles size is around

100 Å [3]. Nevertheless, all of these particles, independent of the size, are catalytically actives. On the other hand, the HDS reaction occurs on edges of small slabs of  $MoS_2$  [11,63], therefore, it is reasonable to use only few atoms to model a catalytic active surface.

Following assumptions were considered for the selection of a catalytic model surface: (a) the surface must have vacancies (completely exposed Mo sites), due to a pretreatment with  $H_2$ ; (b) only single slab structures were chosen because the  $MoS_2$  has a laminar structure with weak interlayer interaction (van der Waals interaction); (c) the electroneutrality principle of clusters must be obeyed, therefore, the total clusters charge is zero [3]; and (d) to study the change of Mo–S bond with the cluster size and surroundings, the central Mo atom ( $Mo_C$ ) was chosen because it represent better a real active site than the other Mo atoms.

Almost all clusters used in this work are non-stoichiometric. The non-stoichiometry of the clusters constitutes a frequent problem in the theoretical modeling. Different solutions have been proposed in the literature, for example, to maintain the stoichiometry and the formal charges of the Mo (Mo<sup>4+</sup>) and the S (S<sup>2-</sup>) atoms some authors had used charged clusters



Fig. 1. Draw of the molecular structures used in this work for the linear  $Mo_x S_y$  systems (x = 3; y = 4, 6, 8, 10, 12, 14 and x = 5; y = 12, 14).

such as  $MoS_6^{8-}$  or  $Mo_7S_{24}^{20-}$  [64], but these high negative charges are quite unrealistic [65]. Another adopted solution is to saturate the clusters with H atoms in such way to compensate the negative charge for example the  $Mo_2S_{10}H_{12}$  cluster [66,67]. On the other hand, in a comparative study using DV-X $\alpha$ between the  $Mo_3S_{14}$ ,  $Mo_3S_6$  and  $Mo_5S_{10}$  clusters, Rong and Qin [68] showed that the non-stoichiometry of the Mo/S ratio does not have a strong influence on the electronic properties. Ma and Schobert [41] using ZINDO showed too that the electronic properties of the Mo atoms does not change when going from stoichiometry clusters to non-stoichiometry ones.

From the assumptions mentioned above, two different types of molecular models were selected: linear and non-linear ones. The linear  $Mo_xS_y$  systems (x =3; y = 6, 8, 10, 12, 14 and x = 5; y = 12, 14) are shown in Fig. 1. The difference between clusters is in the coordination of two mono-coordinated S atoms ( $S_{mc}$ ) to the  $Mo_C$  atom. Having in mind that the  $MoS_2$ surface is treated with  $H_2$ , we consider in our models several degrees of desulfurization, from a desulfurized surface ( $Mo_3S_4$ ) to a total sulfurized surface ( $Mo_3S_{14}$ ), as well as to intermediate cases. Different types of sulfur were included in the models: mono-coordinated on the border above the cluster ( $S_{mb}$ ), on the edge below ( $S_{me}$ ), and the bridge ( $S_b$ ) bi-coordinated.

In the case of non-linear systems,  $Mo_x S_y$  (x = 3, y = 6, 8, and x = 5, y = 6, 8, 10, 12, 14, 16, 18, 20), a systematic construction of aggregates were also performed. Fig. 2 displays the non-linear systems studied herein. In these models, two rows of Mo atoms and two or three rows of S atoms were used. Three Mo and six S atoms compose the core of the non-linear system, forming a hexagon which have the correct stoichiometric formula (see Fig. 2).

## 4. Results and discussion

### 4.1. Linear clusters

Several non-stoichiometric molecular clusters with three and five Mo atoms and different sulfur contents were analyzed. The study was done starting from a totally desulfurized surface (Mo<sub>3</sub>S<sub>6</sub>, Mo-terminated ( $30\bar{3}0$ ) edges), to a totally sulfurized one (Mo<sub>3</sub>S<sub>14</sub>, S-terminated ( $10\bar{1}0$ ) edges). All of these linear structures (see Fig. 1) have an optimal spin multiplicity of five, except Mo<sub>3</sub>S<sub>8</sub> and Mo<sub>3</sub>S<sub>12</sub> that are triplet and septuplet, respectively.

Several features can be obtained from Table 1: (a) distances  $R(Mo-S_{mc})$  and  $R(S_{mc}-S_{mc})$  present small variations with the cluster size; (b) the complete saturated edge sites with sulfur atoms (Mo<sub>3</sub>S<sub>12</sub>) have the longest Mo<sub>C</sub>-S<sub>mc</sub> and the smallest S<sub>mc</sub>-S<sub>mc</sub> distances; (c) PDBE(Mo<sub>C</sub>-S<sub>mc</sub>) values correlate with the  $R(Mo_C-S_{mc})$  distance, i.e. the  $R(Mo_C-S_{mc})$  decreases, as the PDBE(Mo<sub>C</sub>-S<sub>mc</sub>) increases; and (d) the distance  $R(S_{mc}-S_{mc})$  and PDBE(S<sub>mc</sub>-S<sub>mc</sub>) are closer to the anion S<sub>2</sub><sup>--</sup> than the neutral S<sub>2</sub> molecule. These facts suggest that the S<sub>mc</sub> atoms behave like an activated S<sub>2</sub><sup>--</sup> group. A similar structure of S-S bonds was reported for Mo-S and W-S compounds [60].

The bond orders (see Table 2) show that the interaction between the  $S_{mc}$  and  $S_b$ , with the  $Mo_C$  atom is through Mo-sp orbitals with an important participation of metal d orbitals. Free Mo atom has a  $5s^{1}4d^{5}$ configuration. However, in the linear aggregates, the Mo atom has a  $5s^{0.3}5p^{0.3}4d^{4.7}$  configuration. It is clear therefore, that a charge transfer from Mo to S atoms occurs as well as an electronic reorganization, i.e. an spd re-hybridization. This facilitate the binding of several S atoms to one Mo atom. The central Mo (Mo<sub>C</sub>) is bonded not only to S<sub>mc</sub> and S<sub>b</sub>, but to the neighbor

Table 1 Geometrical properties and PDBE values for  $Mo_C$  and  $S_{\rm mc}$  atoms in linear clusters

| (kcal/mol) |
|------------|
|            |
|            |
|            |
|            |
|            |
|            |
|            |



Fig. 2. Draw of the molecular structures used in this work for the non-linear systems,  $Mo_x S_y$  (x = 3, y = 6, 8, and x = 5, y = 6, 8, 10, 12, 14, 16, 18, 20).

Table 2 Partitioned bond orders (sp-sp and d-sp) for Mo-Mo and Mo-S bonds in linear clusters

| Cluster   | Mo <sub>C</sub> -Mo <sub>N</sub> |              | Mo <sub>C</sub> -S <sub>b</sub> |              | Mo <sub>C</sub> -S <sub>mc</sub> |           | S <sub>mc</sub> -S <sub>mc</sub> |  |
|---|----------------------------------|--------------|---------------------------------|--------------|----------------------------------|-----------|----------------------------------|--|
|   | sp-sp                            | d-sp         | sp-sp                           | d–sp         | sp–sp                            | d–sp      | sp–sp                            |  |
| $Mo_3S_4$   | 0.76                             | 0.06         | 1.02                            | 0.37         | 0.93                             | _         | _                                |  |
| $Mo_3S_6$   | 0.70                             | 0.05         | 0.95                            | 0.39         |                                  | 0.45      | 0.87                             |  |
| $\mathrm{Mo_3S_8}\ \mathrm{Mo_3S_{10}}$                 | 0.74                             | 0.06         | 1.02                            | 0.35         | _                                | -         | _                                |  |
|   | 0.69                             | 0.04         | 0.94                            | 0.39         | 0.94                             | 0.45      | 0.85                             |  |
| $\mathrm{Mo}_5\mathrm{S}_{12}$                          | 0.74                             | 0.07         | 1.02                            | 0.39         | _                                | _         | _                                |  |
| $\mathrm{Mo}_5\mathrm{S}_{14}$                          | 0.69                             | 0.06         | 0.93                            | 0.38         | 0.94                             | 0.40      | 0.76                             |  |
| $\begin{array}{l}Mo_{3}S_{12}\\Mo_{3}S_{14}\end{array}$ | 0.68<br>0.65                     | 0.06<br>0.05 | 0.97<br>0.94                    | 0.35<br>0.35 | $^{-}_{0.88}$                    | _<br>0.38 | _<br>1.04                        |  |

Mo atoms ( $Mo_N$ ) through sp–sp interactions. When the  $Mo_C-S_{mc}$  is formed a weakening of the  $Mo_C-S_b$ and  $Mo_C-Mo_N$  bonds occurs due to the redistribution of the electrons in the bonding structure.

The PDBE values in Table 3 clearly show, as well as the bond order values in the Table 2, that there is a  $Mo_C-Mo_N$  bond that is weaker than the  $Mo_C-S$  bond. The existence of Mo–Mo bond is not unusual, for example, the experimental Mo–Mo bond distance is 3.22 Å in the  $[h^5-C_5H_5Mo(CO)_3]_2$  [69] complex. This distance is longer than the Mo–Mo distance (3.16 Å) in MoS<sub>2</sub> [70]. Therefore, one could expect an Mo–Mo bond in the MoS<sub>2</sub>. Table 3 shows a general tendency, the Mo–S<sub>b</sub> bonds (PDBE(Mo<sub>C</sub>–S<sub>b</sub>)) are stronger than the Mo<sub>C</sub>–S<sub>mc</sub> ones (see Table 1). This result in concordance with the experimental results [37,70], which show that S<sub>mc</sub> atom is more labile than the S<sub>b</sub> ones.

Table 3 PDBEs and net charges on the Mo<sub>C</sub> and the S<sub>mc</sub> atoms for linear clusters

The calculated  $Mo_C-S_{mc}$  (2.27–2.35 Å) bond distances (Table 1) are shorter than those in the  $MoS_2$ bulk (2.41 Å) [71]. This can be explained due to unsaturations in the small clusters sizes. The net charge on the  $Mo_C$  (see Table 3), as expected, increases when the coordination of the  $Mo_C$  atom increases. This shows that an oxidation process occurs on the Mo atom. The total net charge on two  $S_{mc}$  atoms is around -0.6e, indicating again that the  $S_{mc}-S_{mc}$  behaves like an activated  $S_2^-$  group, as shown previously.

Increasing the saturation of the neighbor Mo atoms affect the electronic distribution of the central Mo atom. The PDBE( $Mo_C-Mo_N$ ) is lower for  $Mo_3S_{12}$ than for  $Mo_3S_8$ ,  $Mo_3S_4$ , and  $Mo_5S_{12}$  because the Mo<sub>N</sub> atoms have to share their electrons with the S<sub>mb</sub> atoms. A particular striking result is the interaction Mo<sub>C</sub>-S<sub>mc</sub> in the Mo<sub>3</sub>S<sub>14</sub> molecular cluster. The S<sub>mc</sub> atoms are less bonded to the central Mo in the Mo<sub>3</sub>S<sub>14</sub> than in the other linear clusters. As a consequence, the  $PDBE(S_{mc}-S_{mc})$  is higher and the  $PDBE(Mo_{C}-S_{mc})$ is lower than in the other clusters, see Table 1. For Mo<sub>3</sub>S<sub>14</sub> cluster, the central Mo atom has one unpaired electron, therefore, two Smc atoms are bonded to the Mo<sub>C</sub> through one electron instead of two, as a result the interaction between the Mo<sub>C</sub> and the S<sub>mc</sub> atoms is weaker.

The interaction between the central Mo and the S atoms can be analyzed as a reaction between one  $S_2$  molecule with a clean  $MoS_2$  surface, according to the following reactions scheme:

$$Mo_3S_8 + S_2 \to Mo_3S_{10},$$
  

$$\Delta E = -141.1 \text{ kcal/mol}$$
(7)

| Cluster                        | PDBE(Mo <sub>C</sub> -Mo <sub>N</sub> )<br>(kcal/mol) | PDBE(Mo <sub>C</sub> –S <sub>b</sub> )<br>(kcal/mol) | PDBE[Mo–S] <sup>a</sup><br>(kcal/mol) | Charge on Mo <sub>C</sub> | Charge on S <sub>mc</sub> |
|--------------------------------|---|--|---------------------------------------|---------------------------|---------------------------|
| Mo <sub>3</sub> S <sub>4</sub> | -76.0   | -115.3   | -114.7                                | +0.75                     | _                         |
| $Mo_3S_6$                      | -54.5   | -93.3  | -93.7                                 | +1.50                     | -0.30                     |
| Mo <sub>3</sub> S <sub>8</sub> | -55.8   | -94.2  | -93.1                                 | +0.68                     | _                         |
| $Mo_3S_{10}$                   | -59.8   | -92.1  | -92.7                                 | +1.50                     | -0.28                     |
| $Mo_5S_{12}$                   | -52.1   | -95.6  | -98.5                                 | +0.78                     | _                         |
| $Mo_5S_{14}$                   | -48.2   | -89.7  | -92.9                                 | +1.39                     | -0.24                     |
| $Mo_3S_{12}$                   | -46.4   | -94.5  | -96.7                                 | +0.74                     | _                         |
| $Mo_3S_{14}$                   | -41.9   | -92.3  | -90.7                                 | +1.46                     | -0.28                     |

<sup>a</sup> Mean value of the PDBE(Mo-S) in the cluster.

$$Mo_3S_{12} + S_2 \rightarrow Mo_3S_{14},$$
  

$$\Delta E = -124.5 \text{ kcal/mol}$$
(8)

Again, the saturation with S atoms of the neighbor Mo atoms drastically affect the properties of the linear model, lowering the adsorption energy (reaction (8)). This shows the importance of the neighbor atoms. The quantum properties of Mo<sub>3</sub>S<sub>8</sub>, model corresponds to a clean Mo surface in the  $(3 \ 0 \ \overline{3} \ 0)$  plane of the MoS<sub>2</sub>, while the properties and the DE of Mo<sub>3</sub>S<sub>12</sub> to Mo<sub>3</sub>S<sub>14</sub> correspond to the  $(1 \ 0 \ \overline{1} \ 0)$  plane. From the analysis of reaction energies, it is clear that the adsorption of a S<sub>2</sub> molecule is stronger in the  $(3 \ 0 \ \overline{3} \ 0)$  plane than in a Mo vacancy localized in the  $(1 \ 0 \ \overline{1} \ 0)$  plane (reactions (7) and (8)).

Considering the following reactions:

$$Mo_3S_8 + 2S_2 \rightarrow Mo_3S_{12},$$
  

$$\Delta E = -280.1 \text{ kcal/mol}$$
(9)

$$Mo_3S_{10} + 2S_2 \rightarrow Mo_3S_{14},$$
  

$$\Delta E = -263.5 \text{ kcal/mol}$$
(10)

From reactions (9) and (10), values of -140.1 and -131.8 kcal/mol for the adsorption energy of one S<sub>2</sub> molecule were obtained. Comparing these values with the adsorption energy of reaction (8), one can observe the effect of the neighbor S atoms in the adsorption process (compare reactions (9) and (10)). On the other hand, plotting the calculated total binding energy (TBE) of the linear structures versus total number of Mo–S bonds, a linear relationship is obtained, as shown in Fig. 3. The value of the slope is -107.6 kcal/mol per bond. This value is higher than most of the average values given in Table 3 because of the formation of S–S bonds and the weakening of Mo–Mo interactions have to be considered.

# 4.2. Non-linear clusters

As in the previous case, a systematic analysis of several non-linear and non-stoichiometric clusters were done. The Mo– $S_{mc}$  and  $S_{mc}$ – $S_{mc}$  distances were only optimized for these clusters (see Fig. 2). In the two rows structures, an optimal multiplicity of three was found, except for the Mo<sub>5</sub>S<sub>18</sub>, which is a quintuplet. Table 4 shows that the interatomic  $S_{mc}$ – $S_{mc}$  and  $Mo_C$ – $S_{mc}$  distances are almost independent of the size of the cluster. In general, the values PDBE for the Mo– $S_{mc}$  and  $S_{mc}$ – $S_{mc}$  bonds are stronger than those found for the linear aggregate models. There is also an important Mo–Mo interaction (see Table 5) that is weaker than in the linear ones.

Two S atoms bonded to the central Mo atom (Mo<sub>C</sub> atom) produces a charge transfer from the Mo atom to the S<sub>mc</sub> atoms, as expected. In this sense, the non-linear clusters the electronic charge density on S atoms is in general, greater than in linear ones, see Table 5. Table 6 shows that the Mo-Mo interaction occurs mainly through the 5s5p orbitals since the 4d orbitals are compromised in the Mo-S bonding. These orbitals represent a 30% of the Mo-S bond through d-sp interactions. A clear decrease of sp-sp and d-sp bond is observed in the non-linear clusters with respect to linear ones. Comparing non-linear with linear structures, the S<sub>mc</sub>-S<sub>mc</sub> bonds are weaker and the negative charge on S<sub>mc</sub> atoms is higher in the former. For example, the Smc-Smc bond order in  $Mo_3S_{14}$  (liner) is 1.04 and 0.88 for  $Mo_5S_{20}$ (non-linear) with  $S_2$  charges of -0.56 and -0.76 a.u., respectively.

Considering the following set of reactions:

$$Mo_3S_6 + S_2 \to Mo_3S_8,$$
  

$$\Delta E = -113.9 \text{ kcal/mol}$$
(11)

Table 4 Geometrical properties and PDBE values for  $Mo_C$  and  $S_{mc}$  atoms in non-linear clusters

| Cluster                        | $R(Mo_C - S_{mc})$ (Å) | $\overline{R(S_{mc}-S_{mc})}$ (Å) | PDBE(Mo <sub>C</sub> -S <sub>mc</sub> ) (kcal/mol) | PDBE(S <sub>mc</sub> -S <sub>mc</sub> ) (kcal/mol) |
|--------------------------------|------------------------|-----------------------------------|--|--|
| Mo <sub>3</sub> S <sub>8</sub> | 2.31                   | 2.16                              | -90.8  | -61.5  |
| $Mo_5S_8$                      | 2.31                   | 2.15                              | -99.5  | -70.7  |
| $Mo_5S_{12}$                   | 2.30                   | 2.16                              | -96.2  | -62.7  |
| $Mo_5S_{16}$                   | 2.29                   | 2.16                              | -96.4  | -60.7  |
| $Mo_5S_{20}$                   | 2.32                   | 2.16                              | -90.0  | -86.7  |
|                                |                        |                                   |  |  |



Fig. 3. Plot of the calculated total binding energy (TBE) of the linear structures vs. total number of Mo-S bonds.

$$\begin{split} \mathrm{Mo}_5\mathrm{S}_6 + \mathrm{S}_2 &\to \mathrm{Mo}_5\mathrm{S}_8, \\ \Delta E &= -153.6\,\mathrm{kcal/mol} \end{split} \qquad \begin{split} \mathrm{Mo}_5\mathrm{S}_{14} + \mathrm{S}_2 &\to \mathrm{Mo}_5\mathrm{S}_{16}, \\ \mathrm{\Delta} E &= -130.8\,\mathrm{kcal/mol} \end{split} \tag{14}$$

 $\begin{aligned} Mo_5 S_{10} + S_2 &\to Mo_5 S_{12}, \\ \Delta E &= -174.1 \, \text{kcal/mol} \end{aligned} \tag{13} \qquad \begin{aligned} &\Delta E &= -108.8 \, \text{kcal/mol} \end{aligned} \tag{15}$ 

| TDDEs and net enarges on the trist, 51 and 5100 atoms for non-intent enarges |   |  |                                       |                           |                           |  |
|--|---|--|---------------------------------------|---------------------------|---------------------------|--|
| Cluster  | PDBE(Mo <sub>C</sub> -Mo <sub>N</sub> )<br>(kcal/mol) | PDBE(Mo <sub>C</sub> -S <sub>T</sub> )<br>(kcal/mol) | PDBE[Mo–S] <sup>a</sup><br>(kcal/mol) | Charge on Mo <sub>C</sub> | Charge on S <sub>mc</sub> |  |
| Mo <sub>3</sub> S <sub>6</sub>   | _   | _  | -90.8                                 | +0.89                     | _                         |  |
| $Mo_3S_8$  | -   | -  | -88.7                                 | +1.39                     | -0.25                     |  |
| Mo <sub>5</sub> S <sub>6</sub>   | -55.6   | -88.7  | -93.1                                 | +0.64                     | _                         |  |
| $Mo_5S_8$  | -51.5   | -84.1  | -92.7                                 | +1.46                     | -0.38                     |  |
| $Mo_5S_{10}$   | -48.5   | -87.1  | -92.0                                 | +0.65                     | _                         |  |
| $Mo_5S_{12}$   | -44.7   | -82.6  | -88.2                                 | +1.40                     | -0.34                     |  |
| Mo <sub>5</sub> S <sub>14</sub>  | -50.8   | -88.9  | -93.6                                 | +0.59                     | _                         |  |
| $Mo_5S_{16}$   | -42.1   | -83.4  | -89.9                                 | +1.47                     | -0.33                     |  |
| Mo <sub>5</sub> S <sub>18</sub>  | -46.5   | -84.3  | -90.1                                 | +0.69                     | _                         |  |
| $Mo_5S_{20}$   | -34.3   | -84.7  | -91.1                                 | +1.40                     | -0.38                     |  |

PDBEs and net charges on the Mo<sub>C</sub>, S<sub>T</sub> and S<sub>mc</sub> atoms for non-linear clusters

<sup>a</sup> Mean value of the PDBE(Mo-S) in the cluster.

Table 5

It is clear from reactions (11)–(13) that the reaction energy (DE) increases as the size of the aggregate increases. On the other hand, for the set of reactions (13)–(15), the energy reaction decreases as the S content increase in the clusters. It shows that increasing the saturation with S atoms affect the chemical properties, such as the reaction energy  $Mo_x S_y + S_2$ .

In similar way, a plot of the calculated total binding energy (TBE) for the non-linear structures versus the total number of Mo–S bonds shows a linear relation (see Fig. 4). The value of the slope –118.6 kcal/mol per bond corresponds to the formation energy of one Mo–S bond. This value is higher than the corresponding of the clusters of the linear structures, because

Table 6 Partitioned bond orders (sp-sp and d-sp) for non-linear clusters

there is an extra stabilization energy due to the cyclic structure. In the non-linear structures, there are more bonds per atom than in a linear one. For example,  $Mo_3S_6$  and  $Mo_3S_8$  clusters present 10 and 12 Mo–S bonds compared with 12 and 14 bonds of the corresponding non-linear clusters. In addition, there are three-coordinated S atoms and two more Mo interactions in clusters of five Mo atoms that help to stabilize these structures. The S–S interactions is important only for edges sulfurs, therefore, if one substract the S–S contributions (half of S–S bond per Mo–S bond) it is possible to make a comparison with the bulk. The average value of S–S bond was -34.1 kcal/mol in  $Mo_5S_{20}$  and result in -84.5 kcal/mol per Mo–S

| Cluster                         | Mo <sub>C</sub> -Mo <sub>N</sub> |      | Mo <sub>C</sub> –S <sub>T</sub> |      | Mo <sub>C</sub> -S <sub>mc</sub> |      | S <sub>mc</sub> -S <sub>mc</sub> |  |
|---------------------------------|----------------------------------|------|---------------------------------|------|----------------------------------|------|----------------------------------|--|
|                                 | sp-sp                            | d–sp | sp-sp                           | d–sp | sp-sp                            | d–sp | sp–sp                            |  |
| Mo <sub>3</sub> S <sub>6</sub>  | _                                | _    | 1.00                            | 0.32 | _                                | _    | _                                |  |
| $Mo_3S_8$                       | _                                | _    | 0.92                            | 0.38 | 0.97                             | 0.41 | 0.83                             |  |
| Mo <sub>5</sub> S <sub>6</sub>  | 0.67                             | 0.06 | 0.92                            | 0.34 | _                                | _    | _                                |  |
| $Mo_5S_8$                       | 0.63                             | 0.04 | 0.84                            | 0.33 | 0.94                             | 0.41 | 0.92                             |  |
| Mo <sub>5</sub> S <sub>10</sub> | 0.67                             | 0.04 | 0.93                            | 0.32 | _                                | _    | _                                |  |
| $Mo_5S_{12}$                    | 0.63                             | 0.04 | 0.83                            | 0.38 | 0.96                             | 0.43 | 0.77                             |  |
| Mo <sub>5</sub> S <sub>14</sub> | 0.71                             | 0.05 | 0.93                            | 0.33 | _                                | _    | _                                |  |
| $Mo_5S_{16}$                    | 0.62                             | 0.04 | 0.84                            | 0.35 | 0.96                             | 0.41 | 0.79                             |  |
| Mo <sub>5</sub> S <sub>18</sub> | 0.63                             | 0.06 | 0.88                            | 0.37 | _                                | _    | _                                |  |
| $Mo_5S_{20}$                    | 0.59                             | 0.05 | 0.82                            | 0.35 | 0.89                             | 0.35 | 0.88                             |  |



Fig. 4. Plot of the calculated total binding energy (TBE) for the two-layer structures vs. the total number of Mo-S bonds.

bond. This value is close to the reported value of -87.9 kcal/mol for the energy of sulfur-extraction calculated by using DFT approach [58].

In order to estimate the energy for the vacancy formation, the reaction

$$\mathrm{Mo}_{n}\mathrm{S}_{m} + \mathrm{H}_{2} \to \mathrm{Mo}_{n}\mathrm{S}_{m-1} + \mathrm{H}_{2}\mathrm{S}$$
(16)

is divided in a two-step reaction. The first correspond to the extraction of one S atom and the second to the  $H_2S$  formation from molecular  $H_2$  and atomic S:

$$\operatorname{Mo}_n S_m \to \operatorname{Mo}_n S_{m-1} + S$$
 (17)

$$S + H_2 \to H_2 S \tag{18}$$

Using the value of the slope of Fig. 4 and the calculated total binding energy for the reaction (18) (-159.8 kcal/mol), we obtain a value of -40.9 kcal/mol for reaction (16). This value is



Fig. 5. Schematic representation of two-layer aggregates HOMO orbital.

higher than the reported using DFT calculations of -30.1 kcal/mol [24].

In general, for non-linear aggregates, the HOMO is highly localized over the S atoms, as shown in Fig. 5. Fig. 5a and b shows that this orbital is the anti-bonding combination of two atomic p-type orbitals that belongs to the  $S_{mc}$  atoms. In the case of totally saturated clusters, the HOMO is delocalized over the whole structure (see Fig. 5c). Since the HOMO is localized in unsaturated aggregates and no localized in saturated aggregates (Fig. 5a and b), the reactivity of both aggregates could be different, but concentrated over the S atoms and not over the metallic centers. Taken into account the localization of the HOMOs and the electronic charge of these S atoms, it is possible to explain, partially, the mechanism of the H<sub>2</sub> dissociation. Since the S<sub>mc</sub> atoms are negatively charged and the HOMO is localized over these atoms, it is very feasible that a charge transfer occurs from the  $S_{mc}$  atoms to the  $H_2$ anti-bonding  $\sigma^*$  orbital, which makes more easy the H<sub>2</sub> dissociation and formation of S-H bond. These results are in agreement with previously published ones [23] that show that the addition of molecular  $H_2$  to two adjacent sulfur atoms is a favorable process. Due to the different shapes of the HOMO in saturated and unsaturated aggregates the mechanism of vacancies formation can be different for both aggregates. For saturated aggregates, the H<sub>2</sub> molecule could first attacks any of S atoms, the S<sub>mc</sub>, S<sub>mb</sub>, S<sub>me</sub>, S<sub>b</sub> and the tricoordinate ones. After the vacancy formation the HOMO change its shape (unsaturated aggregate, Fig. 5a and b), therefore, the H<sub>2</sub> will interact preferentially with the S<sub>mc</sub>.



Fig. 6. Schematic representation of LUMO orbital.

On the other hand, the LUMO orbital is mainly located on the coordinatively unsaturated Mo atoms  $(Mo_N \text{ atoms, see Fig. 6})$ . This indicates that these Mo atoms have electron-accepting properties while the S<sub>mc</sub> atoms, due to the localization of the HOMO, have electron-donating properties. Ma and Schobert [41] using ZINDO program reported that the LUMO orbital of a M<sub>10</sub>S<sub>18</sub> cluster is delocalized over the whole structure, but similar to our results, concentrated on unsaturated Mo atom. They concluded, therefore that the electron-acceptor properties of this atom let the flat adsorption of the thiophene molecule. Both factors (the localization of the HOMO and the LUMO orbitals) help to understand the HDS mechanism. Due to the LUMO is localized over the unsaturated Mo atoms, the thiophene molecule can coordinate to these Mo atoms while the neighbor S atoms can donate charge to the thiophene ring facilitating the breaking of the ring, as shown schematically in Fig. 7.

Delmon and coworkers [33], using ab initio calculations with a small basis set in a  $Mo_{27}S_{54}$  cluster, found that the Mo atoms on the corner have both



Fig. 7. Schematic representation of electron transfer from S atoms to the adsorbed thiophene molecule.

electron-accepting and donating properties, which is in agreement with our results. Nevertheless, they reported that the unsaturated central Mo atom (Mo<sub>C</sub>) has very little participation in the LUMO orbital; therefore, this atom does not have electron-accepting properties. Our results, as well as those of [41], show that the LUMO is mainly localized over all coordinatively unsaturated Mo atoms. This disagreement could be explained by the fact that the semi-empirical approaches include in some degree the electronic correlation [43,46], and ab initio calculations with minimum basis sets are less accurate than semi-empirical ones [72].

# 5. Conclusions

- (a) Once more, the use of energy partition and the parameterization of CNDO method using diatomic binding energies arise as a good tool for studying energetic interactions in catalytic systems.
- (b) The linear clusters are less stable than the non-linear ones, because more bonds per number of atoms are observed in the later. It is convenient to use non-linear clusters with two rows of Mo atom to simulate MoS<sub>2</sub> surface catalyst.
- (c) Changes in PDBEs, bond orders and charges on the Mo and S atoms are, in general, small for different types of aggregates, except for the very unsaturated ones.
- (d) Formation of S–S bonds and S–Mo–S bonds on the surface are important for the formation of vacancies on the surface. It is proposed that a species

of  $S_2^-$  is formed on the  $(10\bar{1}0)$  surface plane. An important Mo–Mo interaction was also found.

- (e) The shape and localization of the HOMO orbital depend on the size and sulfur saturation of clusters. HOMO is localized over the  $S_{mc}$  atoms, which shows that these S atoms are the electron-donating sites of the MoS<sub>2</sub> catalyst.
- (f) The LUMO orbital is delocalized over all unsaturated Mo atoms, therefore, these atoms are principally electron-accepting sites.

#### Acknowledgements

The authors gratefully acknowledged (MTC) G-9700667, S1-2637 (E.N.R-A), CONICIT S1-96001399 grant (A.S.) for the financial support. They also thank Dr. Alejandro Arce for helpful discussions.

#### References

- R. Prins, V.H.J. de Beer, G.A. Somorjai, Catal. Rev.-Sci. Eng. 31 (1989) 1.
- [2] P. Ratnasamy, S. Sivasanker, Catal. Rev.-Sci. Eng. 22 (1980) 401.
- [3] A. Startsev, Catal. Rev.-Sci. Eng. 37 (1995) 353.
- [4] F.E. Massoth, Adv. Catal. 27 (1978) 265.
- [5] X.S. Li, Q. Xin, X.X. Guo, P. Grange, B. Delmon, J. Catal. 137 (1992) 385.
- [6] R.J. Angelici, Polyhedron 16 (1997) 3073.
- [7] S.C. Schuman, H. Shalit, Catal. Rev. 4 (1970) 425.
- [8] R.R. Chianelli, M. Daaage, M.J. Ledoux, Adv. Catal. 40 (1994) 177.
- [9] A.P. Raje, S.-J. Liaw, R. Srinivasan, B.H. Davis, Appl. Catal. A 150 (1997) 297.
- [10] W.K. Hall, in: H.F. Barry, T.C.H. Mitchell (Eds.), Proceedings of the 4th International Conference on the Chemistry, uses if Molybdenum, Climax Molybdenum Co., Ann Arbor, MI, 1982, p. 224.
- [11] K.I. Tanaka, T. Okuhari, J. Catal. 78 (1982) 155.
- [12] B.K. Miremadi, S.R. Morrison, J. Catal. 103 (1987) 334.
- [13] W.P. Dianis, Appl. Catal. 30 (1987) 99.
- [14] T.Y. Park, Y.G. Kim, Ind. Eng. Chem. Res. 36 (1997) 5246.
- [15] M.M. Luchsinger, B. Bozkurt, A. Akgerman, C.P. Janzen, W.P. Addiego, M.Y. Darensbourg, Appl. Catal. 68 (1991) 229.
- [16] L. Artok, O. Erbatur, H.H. Schobert, Fuel Proc. Technol. 47 (1996) 153.
- [17] T.D. Durbin, J.R. Lince, S.V. Didziulis, D.K. Stuck, J.A. Yarmoff, J. Vac. Sci. Technol. A 10 (1991) 2529.
- [18] M. Remskar, A. Mrzel, Z. Skraba, A. Jesih, M. Ceh, J. Demsar, P. Stadelmann, F. Lévy, D. Mihailovic, Science 292 (2001) 479.
- [19] D. Yang, S. Jiménez-Sandoval, W.M.R. Divigalpitiya, J.C. Irwin, R.F. Frindt, Phys. Rev. B 43 (1991) 12053.

- [20] H. Wise, Polyhedron 5 (1986) 145.
- [21] W.M.R. Divigalpitiya, R.F. Frindt, S.R. Morrison, Science 246 (1989) 369.
- [22] S.Y. Li, J.A. Rodríguez, J. Hrbek, H.H. Huang, G.-Q. Xu, Surf. Sci. 366 (1966) 29.
- [23] A. Sierraalta, F. Ruette, J. Mol. Catal. A 109 (1996) 227.
- [24] L.S. Byskov, B. Hammer, J.K. Nørskov, B.S. Clausen, H. Topsøe, Catal. Lett. 47 (1997) 177.
- [25] K.E. Dungey, M.D. Curtis, J.E. Penner-Hahn, Chem. Mater. 10 (1998) 2152.
- [26] P. Raybaud, J. Hafner, G. Kresse, H. Toulhoat, Phys. Rev. Lett. 80 (1998) 1481.
- [27] P. Raybaud, J. Hafner, G. Kresse, H. Toulhoat, Surf. Sci. 407 (1998) 237.
- [28] H. Toulhoat, P. Raybaud, S. Kasztelan, G. Kresse, J. Hafner, Catal. Today 50 (1999) 629.
- [29] J. Heising, M.G. Kanatzidis, J. Am. Chem. Soc. 121 (1999) 638.
- [30] L.S. Byskov, J.K. Nørskov, B.S. Clausen, H. Topsøe, Catal. Lett. 64 (2000) 95.
- [31] V. Alexiev, R. Prins, T. Weber, Phys. Chem. Chem. Phys. 2 (2000) 1815.
- [32] S. Cristol, J.F. Paul, E. Payen, D. Bougeard, S. Clémendot, F. Hutschka, J. Phys. Chem. B 104 (2000) 11200.
- [33] Y.-W. Li, X.-Y. Pang, B. Delmon, J. Phys. Chem. 104 (2000) 11375.
- [34] M. Breysse, G. Berhault, S. Kasztelan, M. Lacroix, F. Maugé, G. Perot, Catal. Today 66 (2001) 15.
- [35] A. Sierraalta, A. Herize, R. Añez, J. Phys. Chem. A 105 (2001) 6519.
- [36] S. Kasztelan, H. Toulhoat, J. Grimblot, J.P. Bonnelle, Appl. Catal. 13 (1984) 127.
- [37] A. Wambeke, L. Jalowiecki, S. Kasztelan, J. Grimblot, J.P. Bonnelle, J. Catal. 109 (1988) 320.
- [38] E. Diemann, Th. Weber, A. Müller, J. Catal. 148 (1994) 288.
- [39] M.C. Zerner, in: K.B. Lipkowistz, D.B. Boyd (Eds.), Reviews in Computational Chemistry, vol. 2, VCH, New York, 1990.
- [40] F. Ruette, A. Sierraalta, A. Hernández, in: F. Ruette (Ed.), Quantum Chemistry Approaches to Chemisorption, Heterogeneous Catalysis, Kluwer Academic Publishers, Dordrecht, 1992, p. 320, references therein.
- [41] X. Ma, H.H. Schobert, J. Mol. Catal. A 160 (2000) 409.
- [42] M. Romero, J. Primera, M. Sánchez, A. Sierraalta, S. Brassesco, J. Bravo, F. Ruette, Folia Chim. Theor. Latina 23 (1995) 45.
- [43] M. Romero, M. Sánchez, A. Sierraalta, L. Rincón, F. Ruette, J. Chem. Inform. Comput. Sci. 39 (1999) 543.
- [44] J. Primera, M. Sánchez, M. Romero, A. Sierraalta, F. Ruette, J. Mol. Struct. (Theochem.) 469 (1999) 177.
- [45] F. Ruette, F.M. Poveda, A. Sierraalta, M. Sánchez, E.N. Rodríguez-Arias, J. Mol. Catal. A: Chem. 119 (1997) 335.
- [46] F. Ruette, C. González, A. Octavio, J. Mol. Struct. (Theochem.) 537 (2001) 17.
- [47] L. Rodríguez, F. Ruette, J. Mol. Struct. (Theochem.) 287 (1993) 179.
- [48] F. Ruette, F.M. Poveda, A. Sierraalta, J. Rivero, Surf. Sci. 249 (1996) 241.

- [49] J.A. Pople, D.L. Beveridge, Approximate Molecular Orbital Theory, McGraw-Hill, New York, 1970.
- [50] A.J. Hernández, F. Ruette, E.V. Ludeña, J. Mol. Catal. 39 (1987) 21.
- [51] F. Ruette, G.L. Estiú, A.J. Jubert, R. Pis-Diez, Rev. Ven. Soc. Catal. 57 (1999) 13.
- [52] F. Ruette, N. Valencia, R. Sánchez-Delgado, J. Am. Chem. Soc. 111 (1989) 40.
- [53] A.E. Gaínza, E.N. Rodríguez, F. Ruette, J. Mol. Catal. 85 (1993) 345.
- [54] E.N. Rodríguez-Arias, A.E. Gainza, A.J. Hernández, P.S. Lobos, F. Ruette, J. Mol. Catal. A: Chem. 102 (1995) 163.
- [55] B. Griffe, A. Sierraalta, F. Ruette, J.L. Brito, J. Mol. Catal. 168 (2001) 265.
- [56] P.M. Atha, L.H. Hillier, M.F. Guest, Chem. Phys. Lett. 75 (1980) 84.
- [57] R.C. Weast (Ed.), Handbook of Chemistry, Physics, 53rd Edition, CRC Press, Cleveland, OH, 1973, p. F-183.
- [58] H. Topsoe, B.S. Clausen, N.Y. Topsoe, J.K. Norskov, C.V. Ovesen, C.J.H. Jacobsen, Bull. Soc. Chim. Belg. 104 (1995) 283.
- [59] J.E. Huheey, Inorganic Chemistry Principles of Structure and Reactivity, Harper & Row, New York, 1975, p. 692.

- [60] A. Müller, Polyhedron 5 (1986) 323.
- [61] E. Diemann, A. Branding, A. Müller, Bull. Soc. Chim. Belg. 100 (1991) 961.
- [62] V.P. Fedin, J. Czyzniewska, R. Prins, T. Weber, Appl. Catal. A 213 (2001) 259.
- [63] S. Helveg, J.V. Lauritsen, E. Lægsgaard, I. Stengaard, J.K. Nørskov, B.S. Clausen, H. Topsøe, F. Besenbacher, Phys. Rev. Lett. 84 (2000) 951.
- [64] A.B. Anderson, Z.Y. Al-Saigh, W.K. Hall, J. Phys. Chem. 92 (1988) 809.
- [65] Y.-W. Li, X.-Y. Pang, B. Delmon, J. Mol. Catal. A: Chem. 169 (2001) 259.
- [66] I.I. Zakharov, A.N. Startsev, G.M. Zhidomirov, J. Mol. Catal. A: Chem. 119 (1997) 437.
- [67] I.I. Zakharov, A.N. Startsev, J. Phys. Chem. B 104 (2000) 9025.
- [68] C. Rong, X. Qin, J. Mol. Catal. 64 (1991) 321.
- [69] F.A. Cotton, G. Wilkinson, Advanced Inorganic Chemistry, 3rd Edition, Interscience, New York, 1972, p. 548.
- [70] L. Jalowiecki, A. Aboulaz, S. Kasztelan, J. Grimblot, J.P. Bonnelle, J. Catal. 102 (1989) 108.
- [71] A. Wold, K. Dwight, Solid State Chemistry, Chapman & Hall, New York, 1993, p. 186.
- [72] M. Karplus, J. Phys. Chem. 94 (1990) 5435.